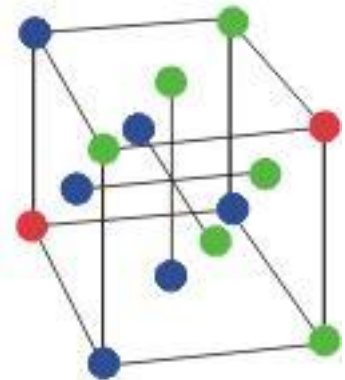
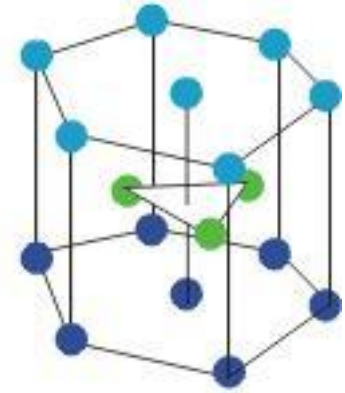
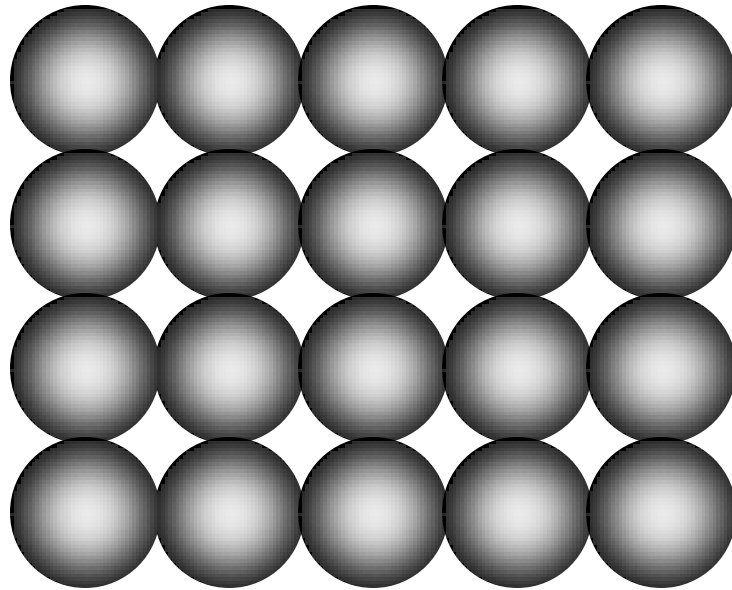


# CLOSE PACKING GEOMETRY

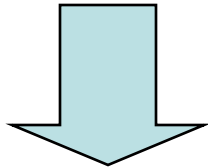


# Packing types

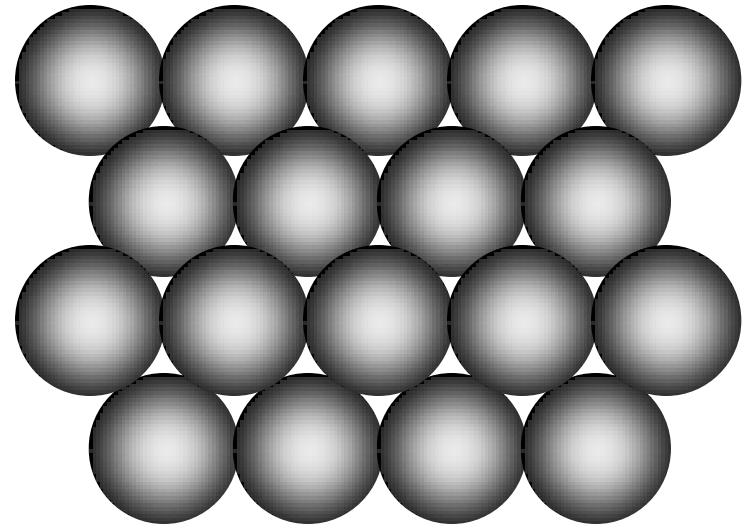


**SIDE BY SIDE**

**PACKING**

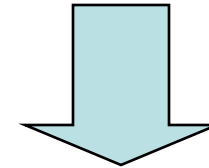


**NOT A CLOSEST  
PACKING**



**HEXAGONAL**

**PACKING**



**CLOSEST  
PACKING**



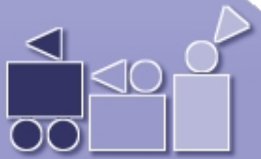
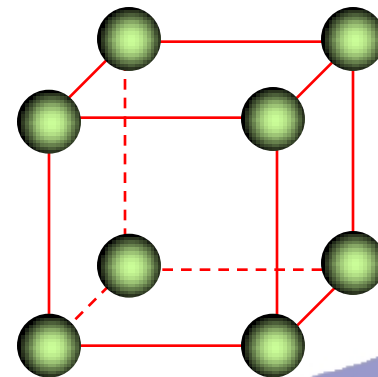
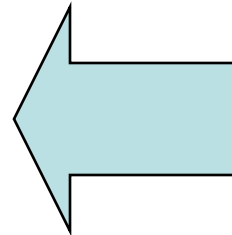
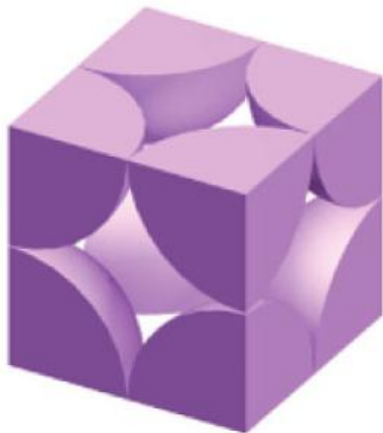
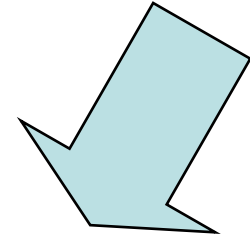
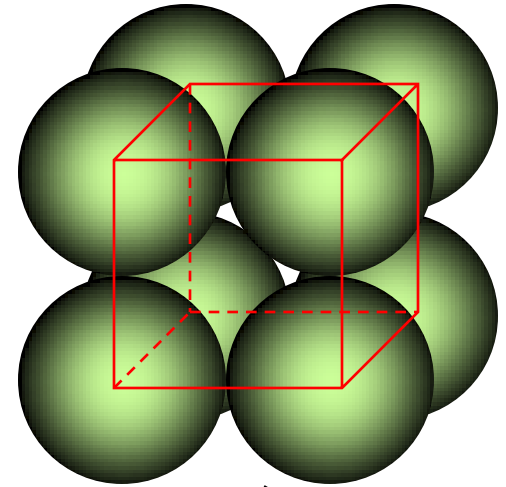
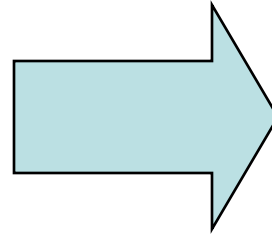
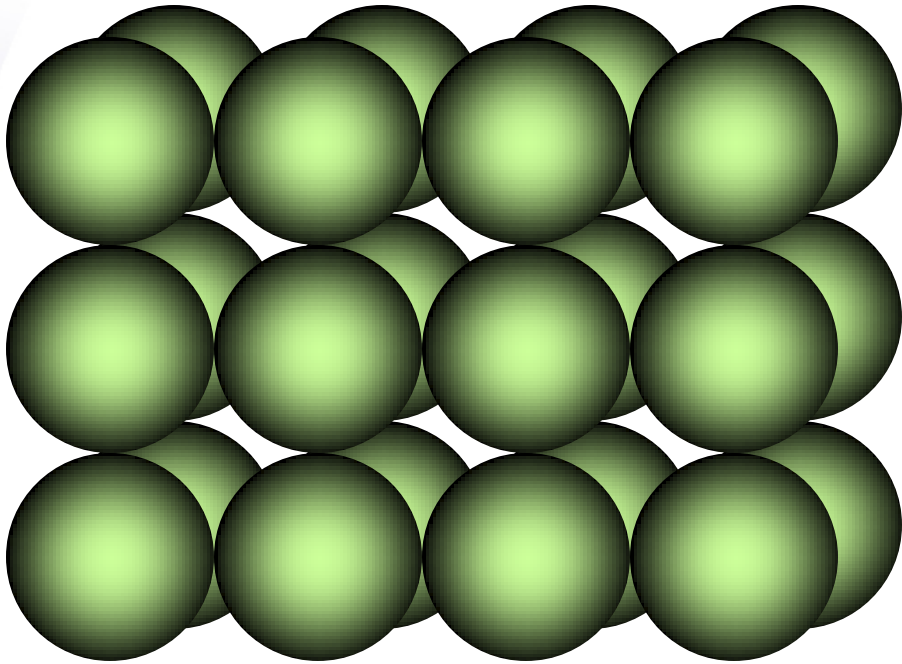
Expanding of side-by-side packing types

1. SIMPLE (PRIMITIVE) CUBIC (SC)

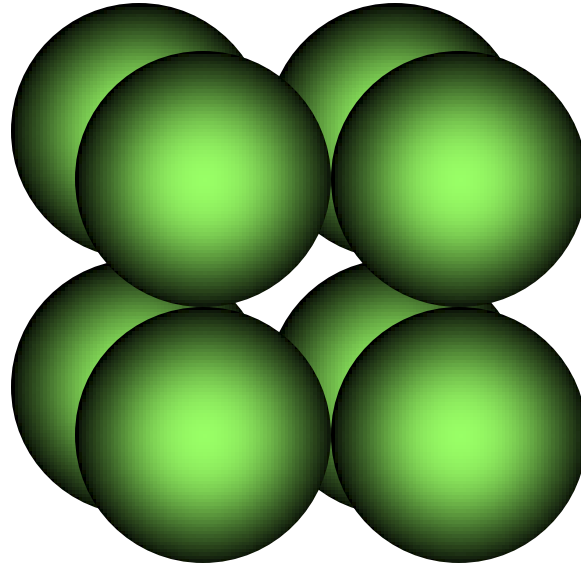
1. BODY CENTERED CUBIC (BCC)



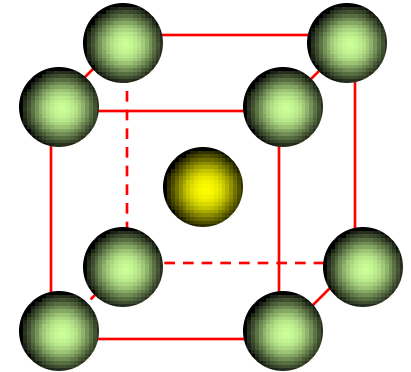
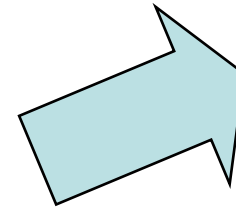
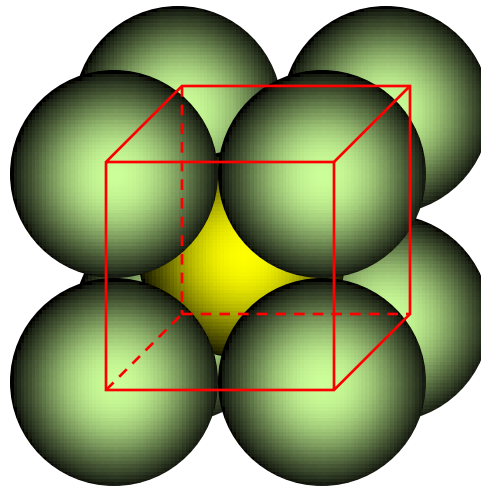
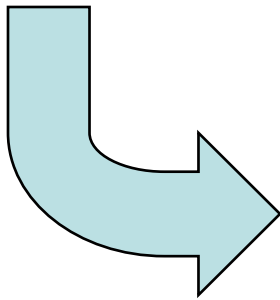
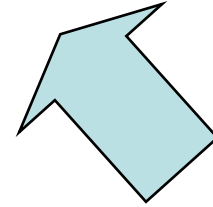
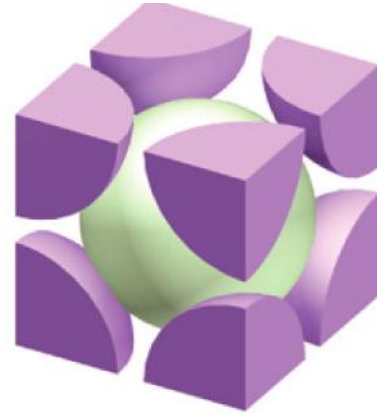
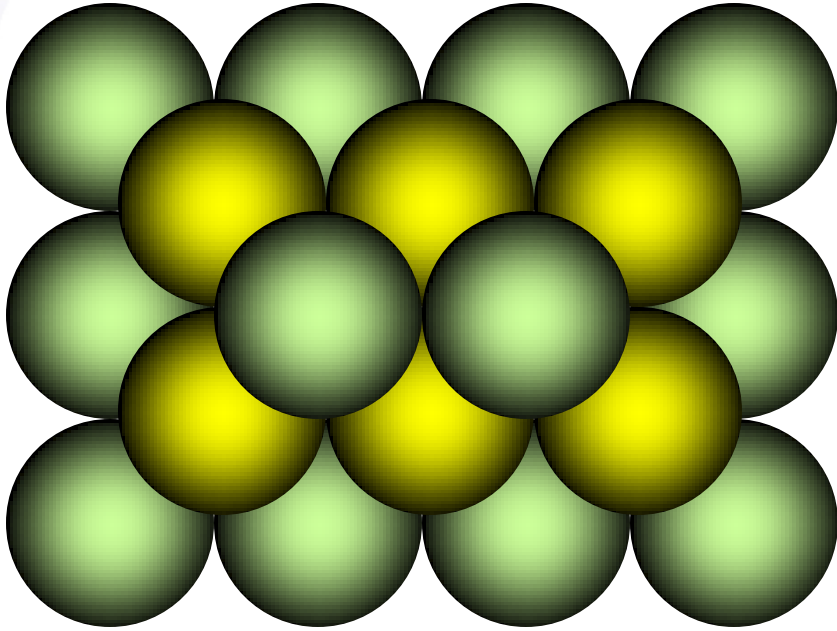
# SIMPLE CUBIC (SC)



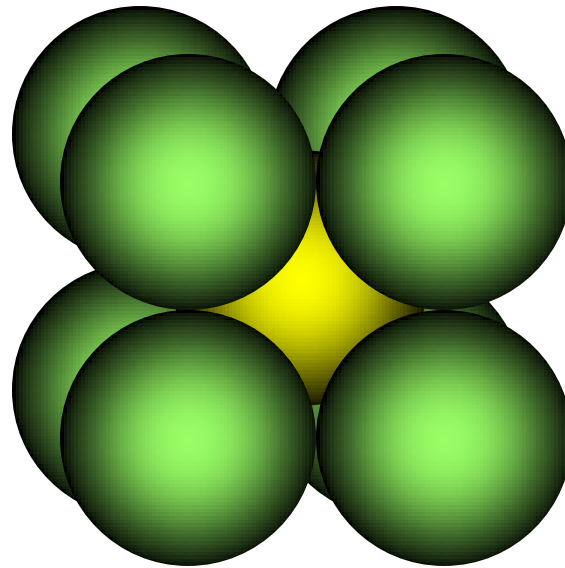
# 1. SIMPLE CUBIC (SC)



## 2. BODY CENTERED CUBIC (BCC)



## 2. BODY CENTERED CUBIC (BCC)



# Hexagonal packing

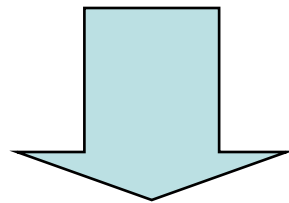
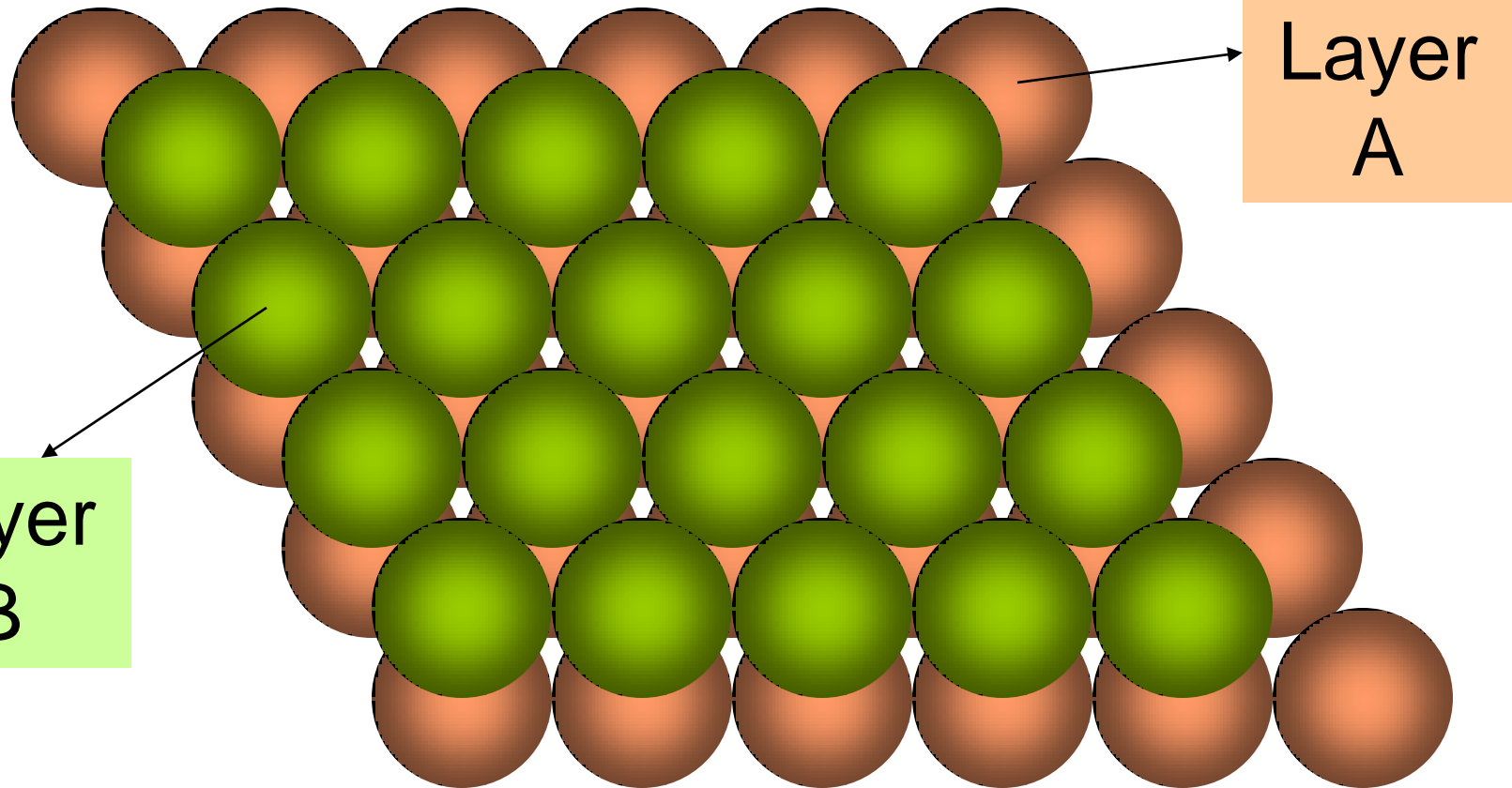
Expanding of hexagonal packing types

1. HEXAGONAL CLOSE PACKING (HCP)
2. CUBIC CLOSE PACKING (CCP or FCC)

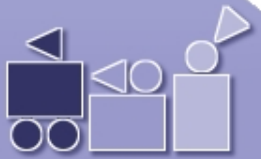




# Close Packing First and Second Layers

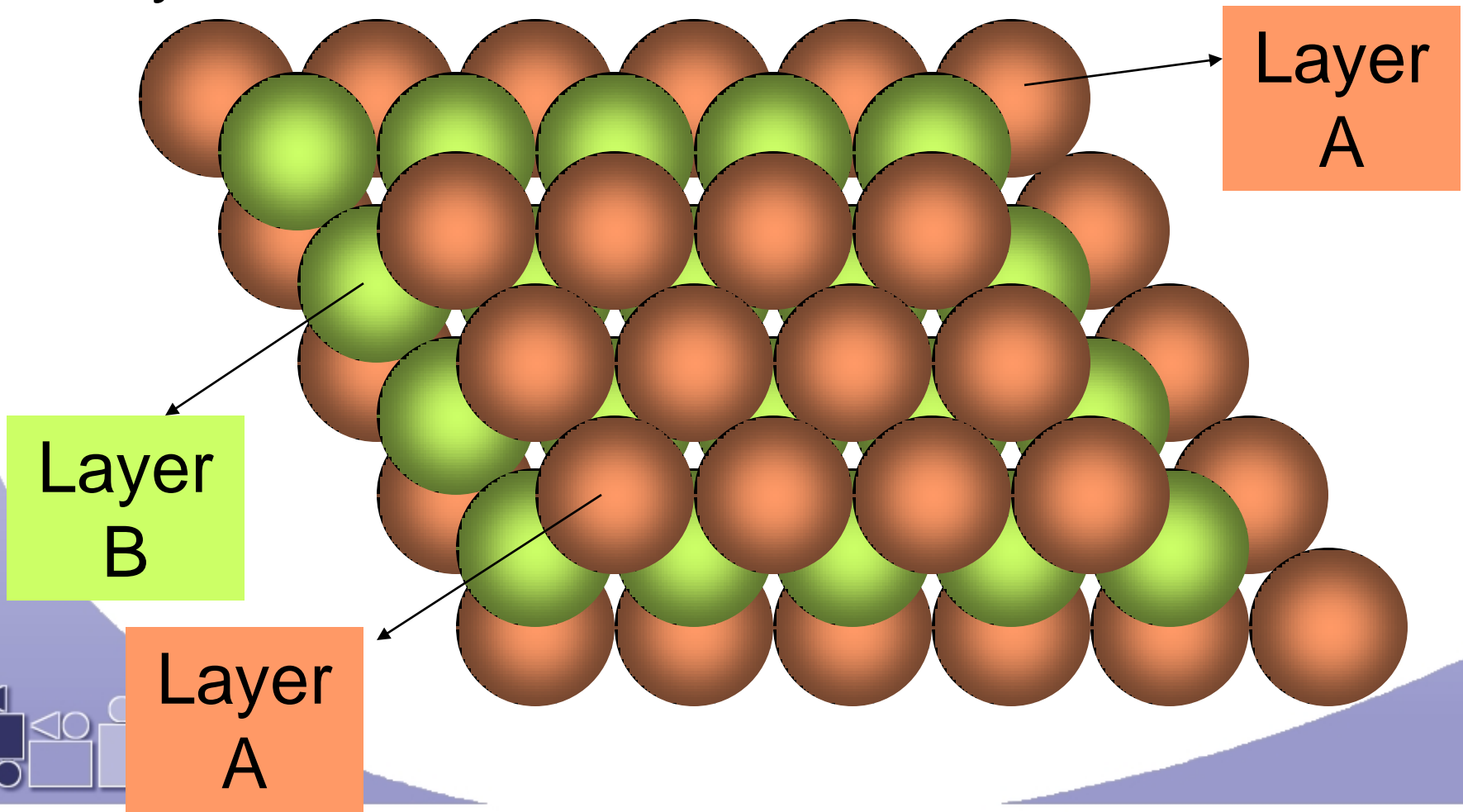


Third layer can then be added in 2 ways:



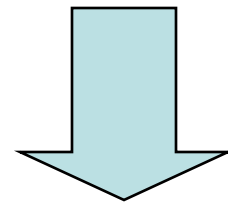
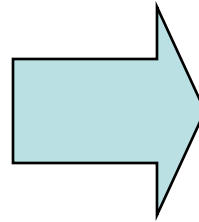
# 1. Hexagonal Close Packing (HCP)

- The third layer fits into the holes of the B layer such that the atoms lie above those in layer A.



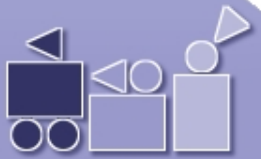
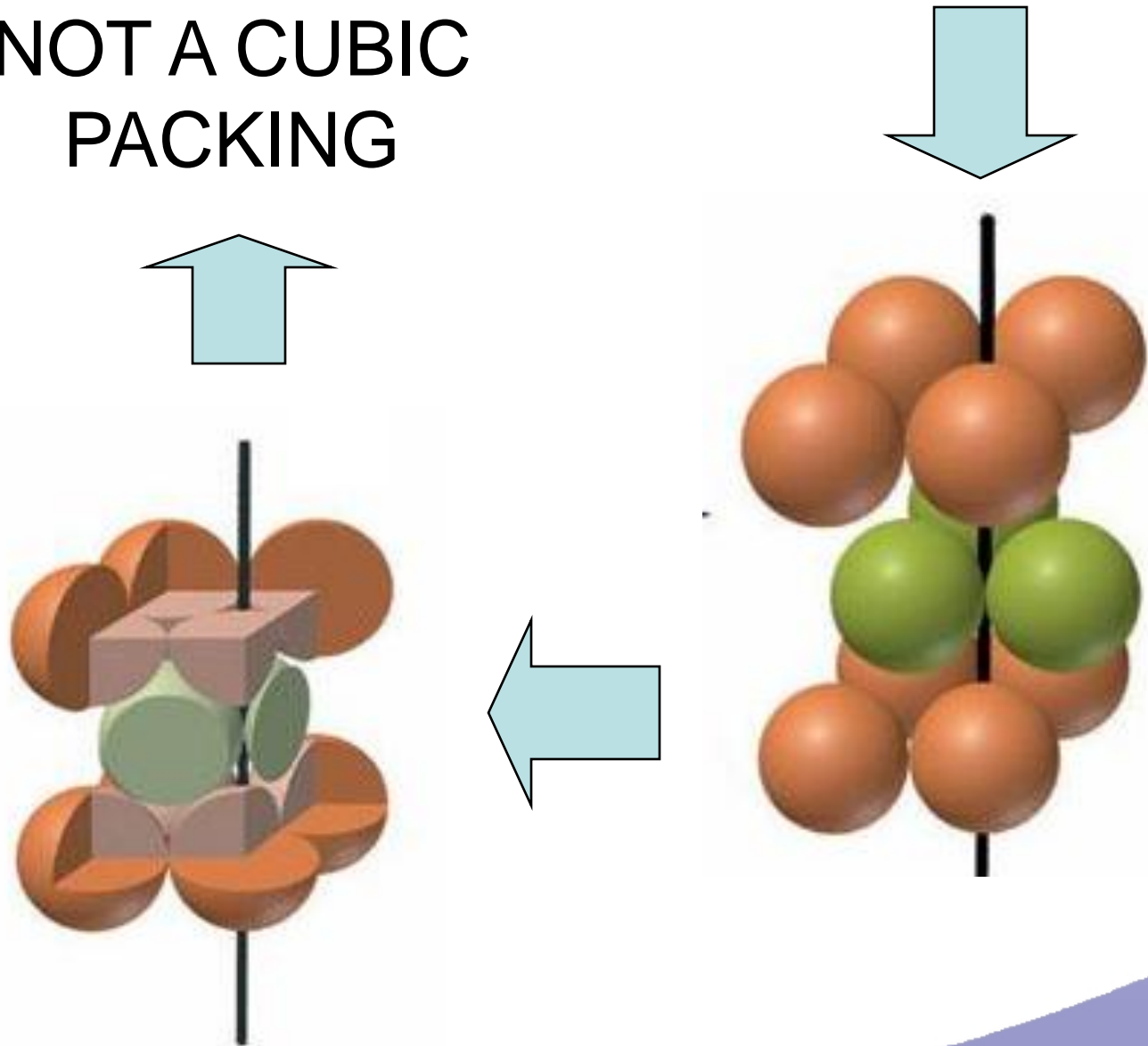
# 1. Hexagonal Close Packing (HCP)

By repeating this arrangement one obtains ABABAB... hexagonal closest packing



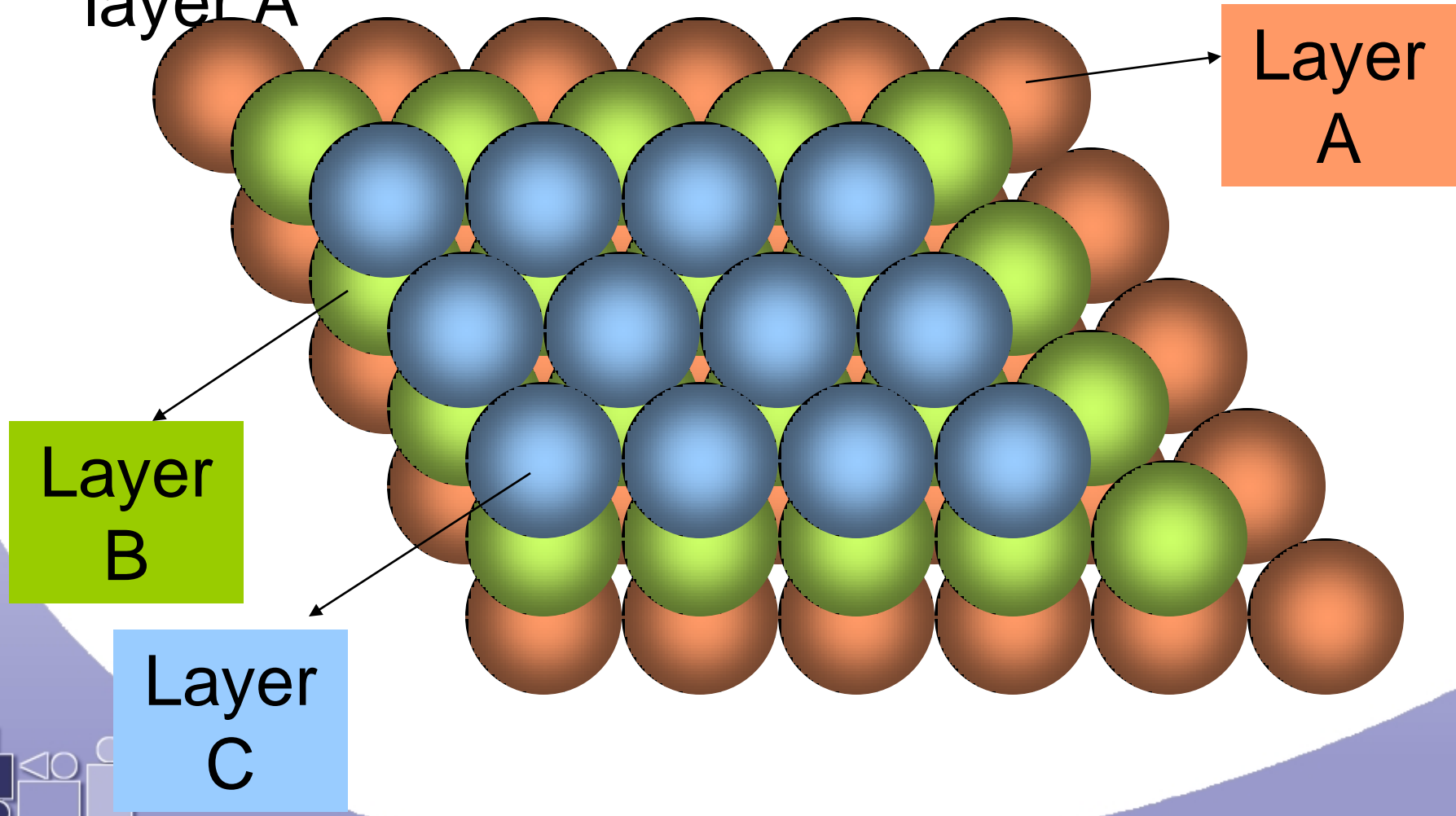
# 1. Hexagonal Close Packing (HCP)

NOT A CUBIC  
PACKING



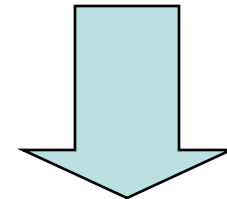
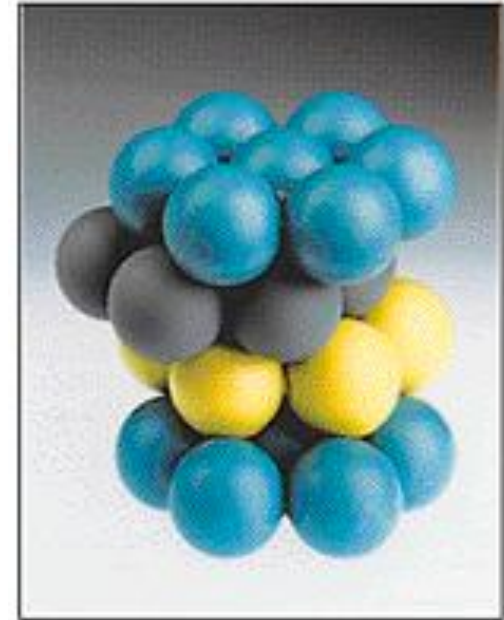
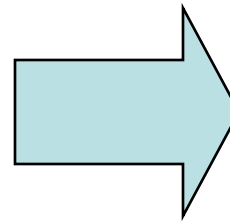
## 2. Cubic Close Packing (CCP or FCC)

- The third layer fits into the holes of the B and the atoms do not lie above those in layer A



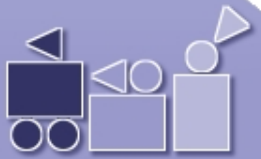
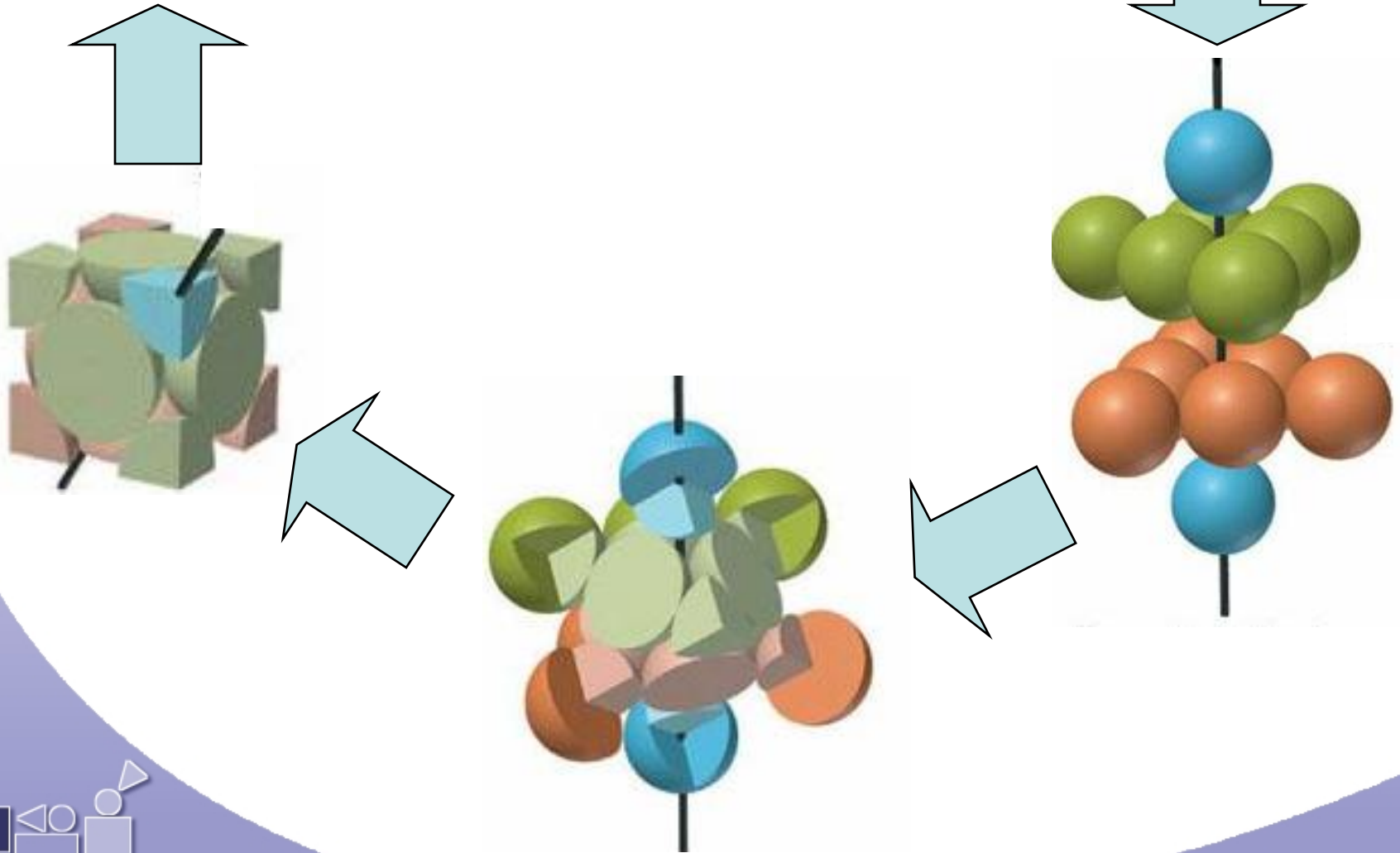
## 2. Cubic Close Packing (CCP or FCC)

By repeating this arrangement one obtains  
ABCABC.....  
cubic closest packing

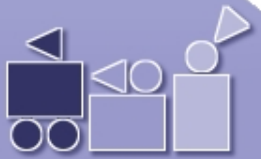
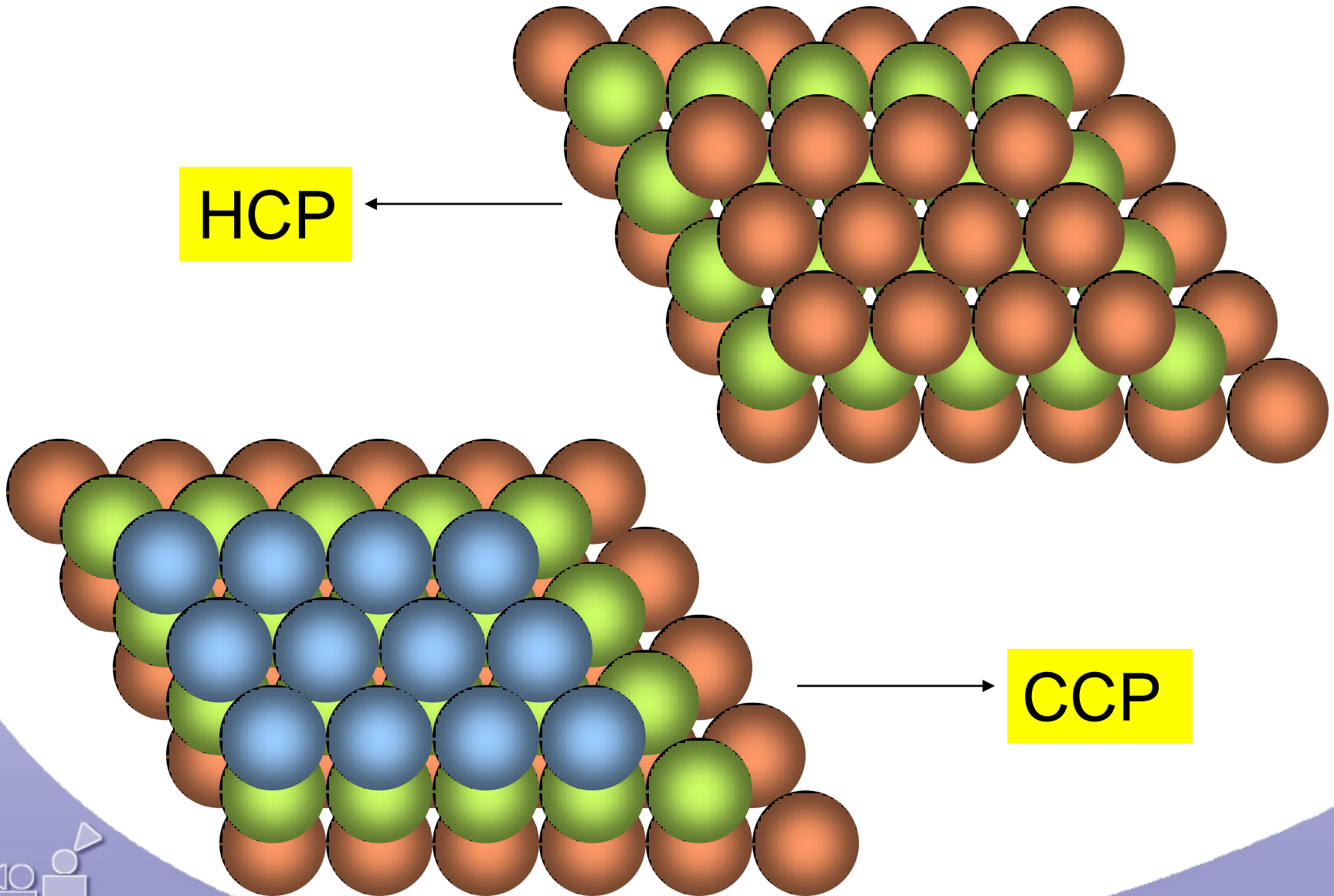


## 2. Cubic Close Packing (CCP or FCC)

A CUBIC PACKING



# Comparison of hcp & ccp





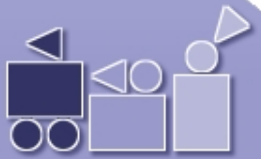
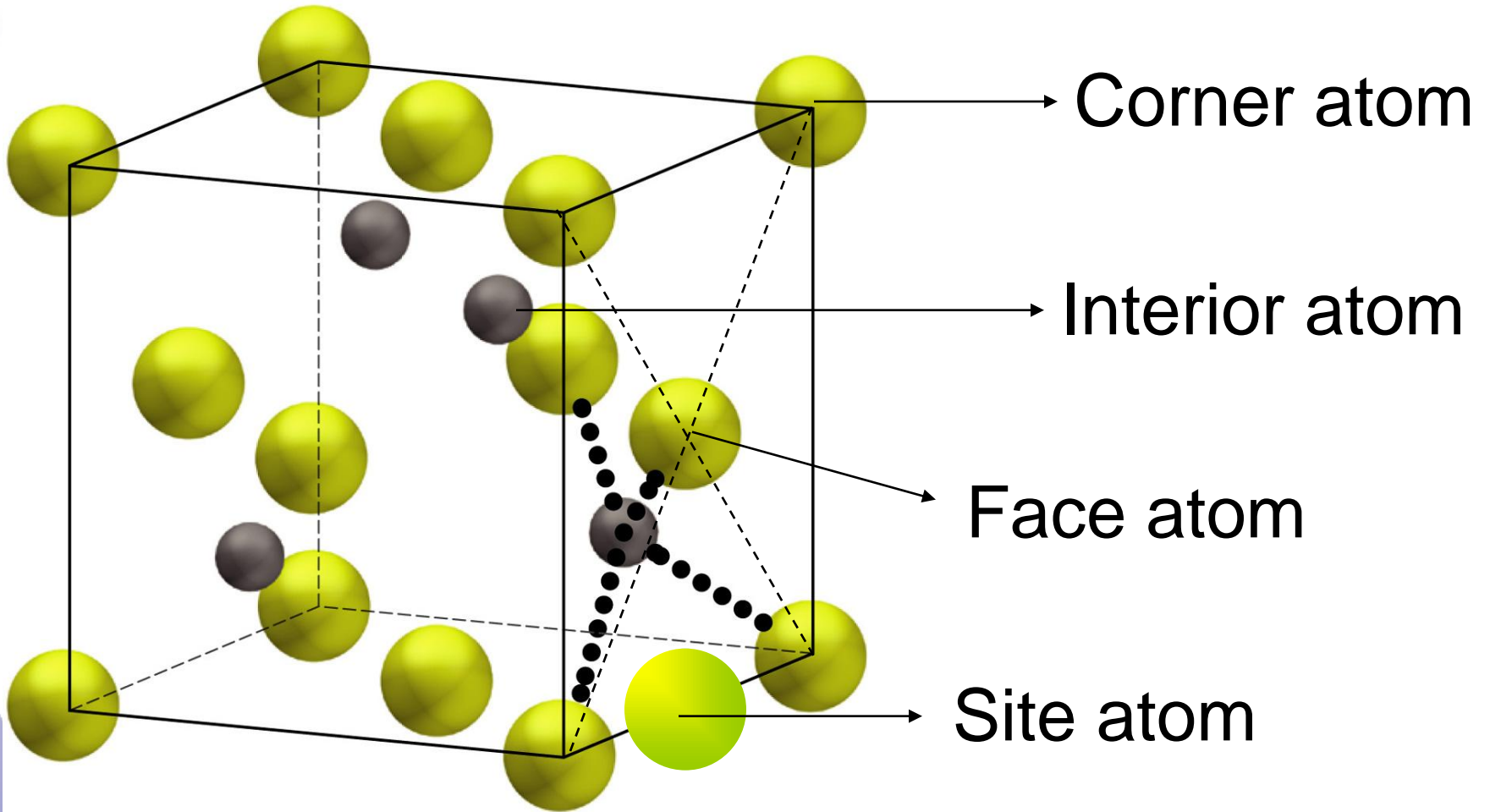
- Unit cell
  - An imaginary parallel-sided region from which the entire crystal can be built up
  - Usually the smallest unit cell which exhibits the greatest symmetry is chosen.
  - If repeated (translated) in 3 dimensions, the entire crystal is recreated.



## Problem 1:

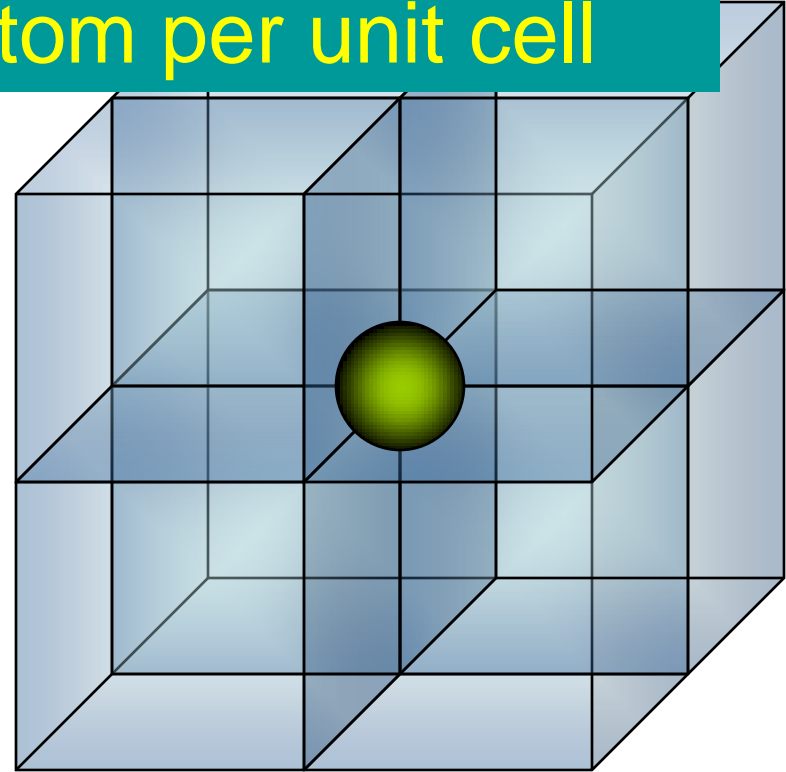
- Determine the number of atom per unit cell, coordination number and packing efficiency of:
  - Simple cubic (SC)
  - Body center cubic (BCC)
  - Face center cubic (FCC)





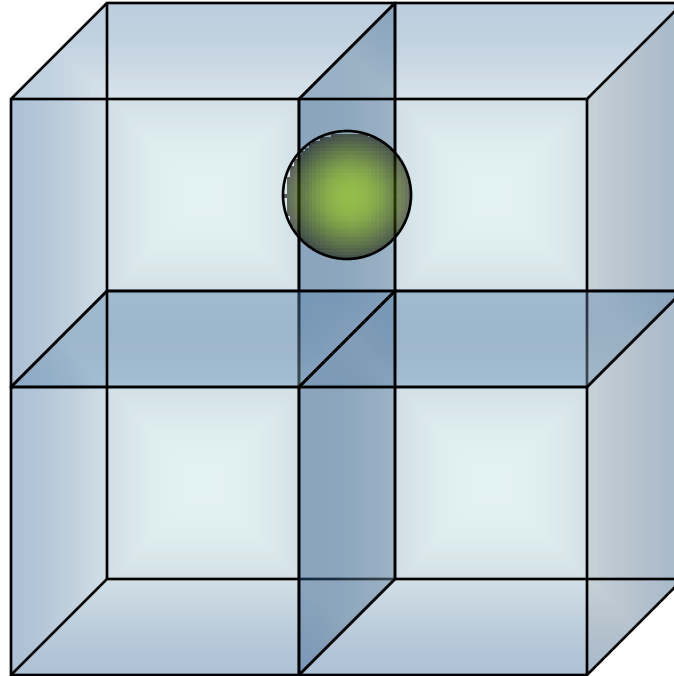
# Corner atom

Corner atom =  $1/8$  atom per unit cell



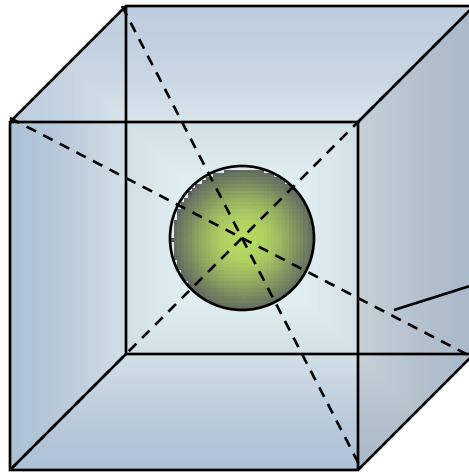
# Face atom

Face atom =  $1/2$  atom per unit cell



# Interior atom

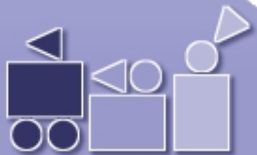
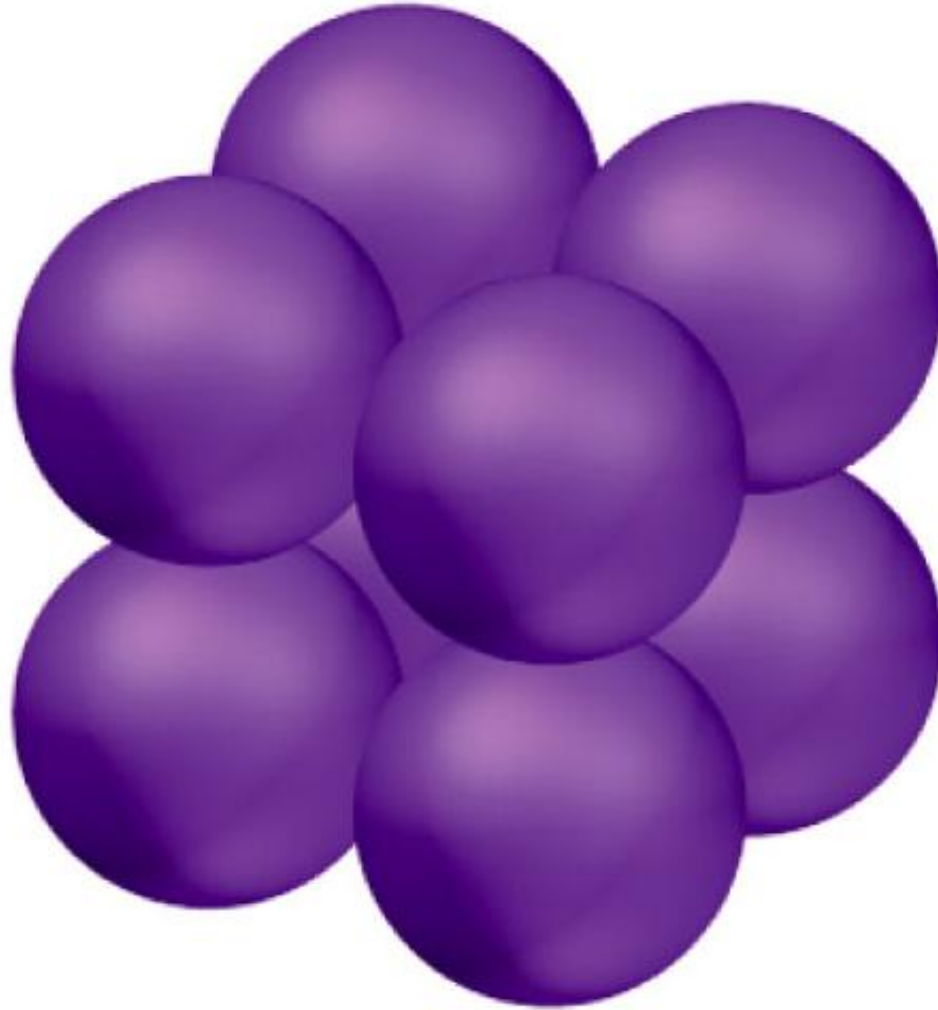
Interior atom = 1 atom per unit cell



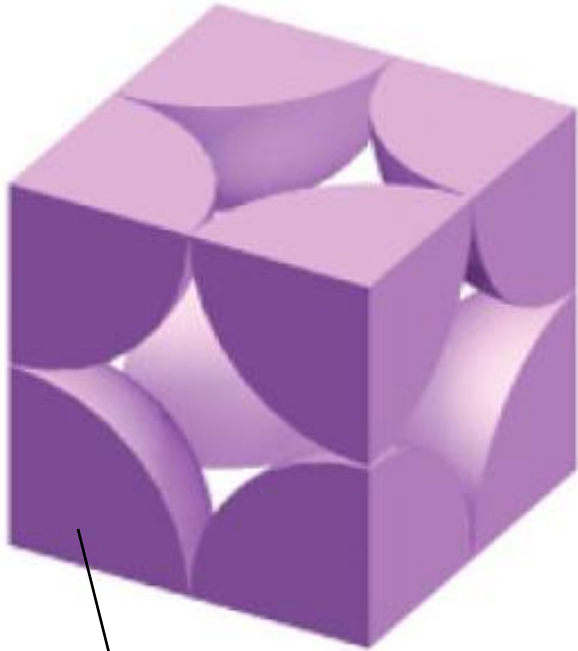
Body diagonal



# Number of Atoms in SC Unit Cell



# Number of Atoms in SC Unit Cell



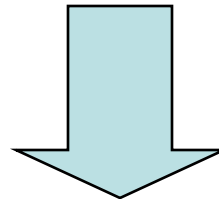
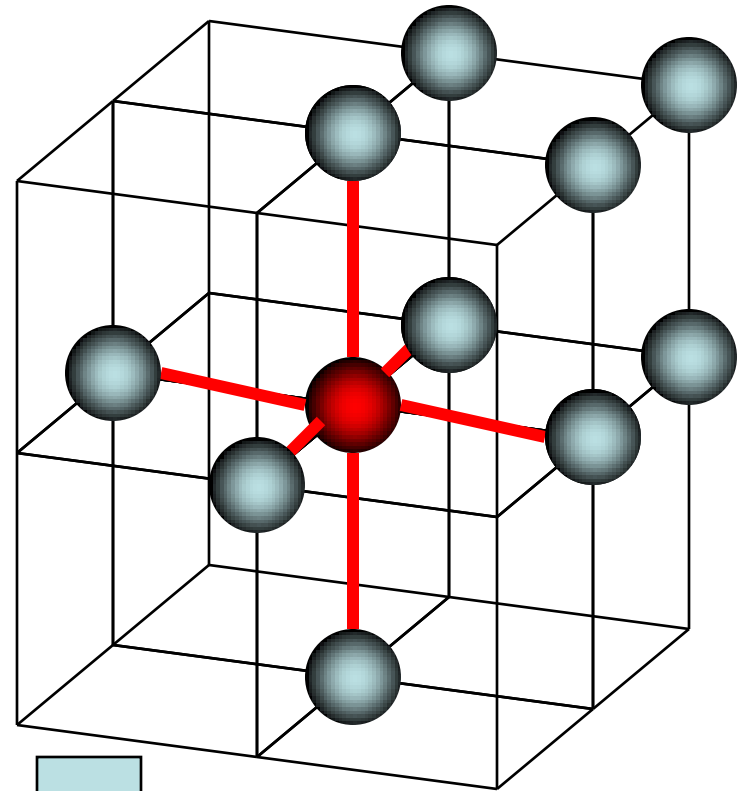
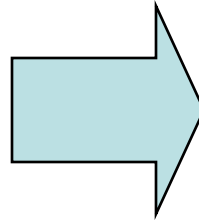
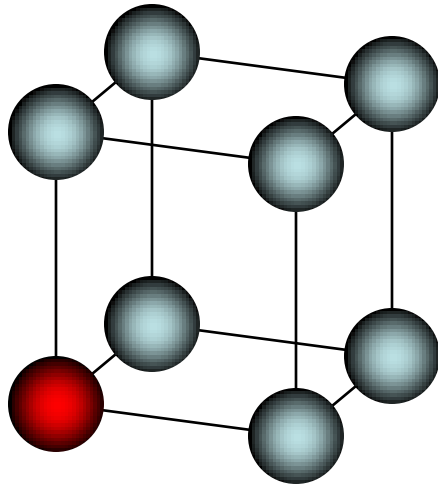
$$\begin{aligned} \text{number of atom} &= \frac{1}{8} \times 8 \text{ corner atoms} \\ &= 1 \text{ atom} \end{aligned}$$

1/8 atom





# Coordination Number of SC



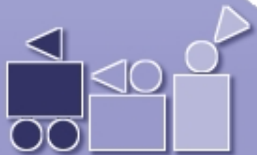
CN OF SC = 6



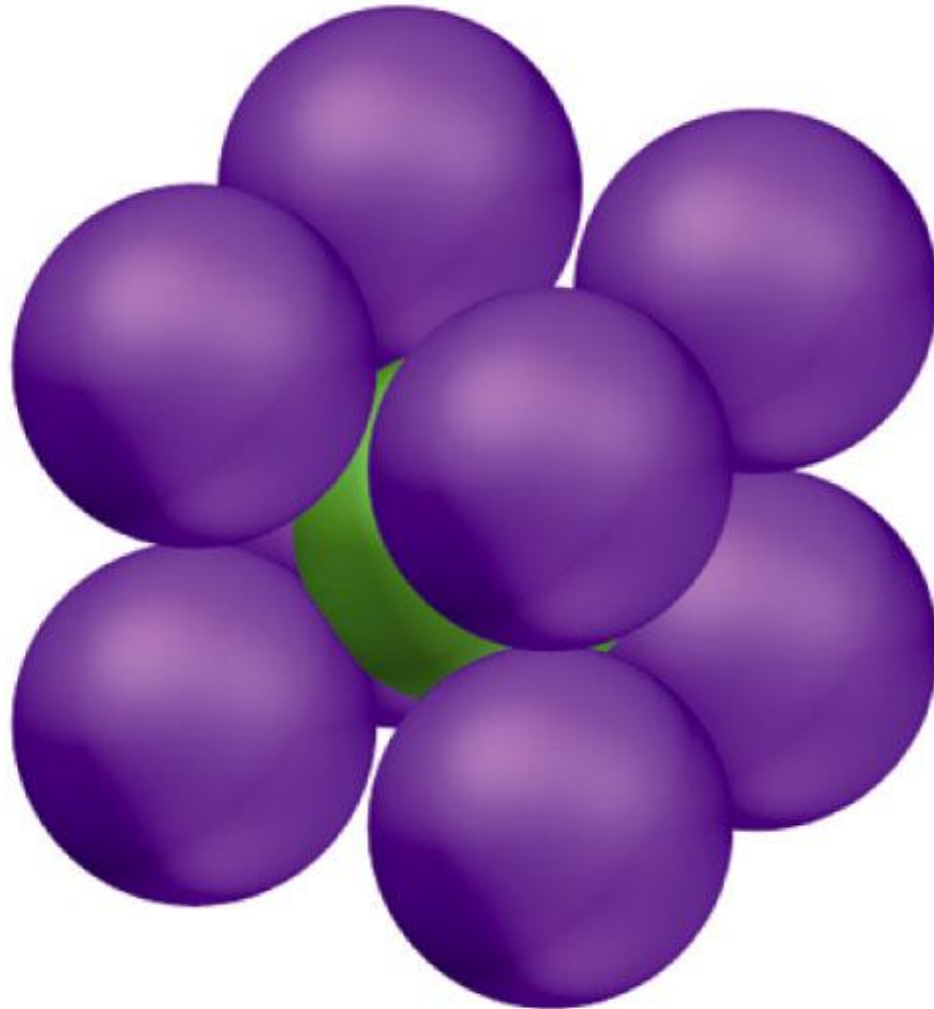
# Packing Efficiency of SC



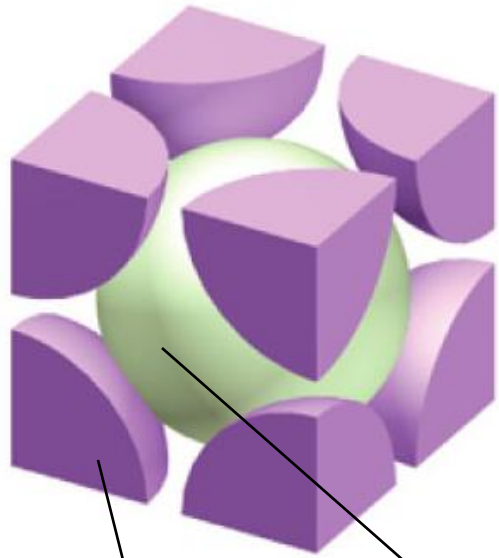
Packing efficiency = 52% ?



# Number of Atoms in BCC Unit Cell



# Number of Atoms in BCC Unit Cell



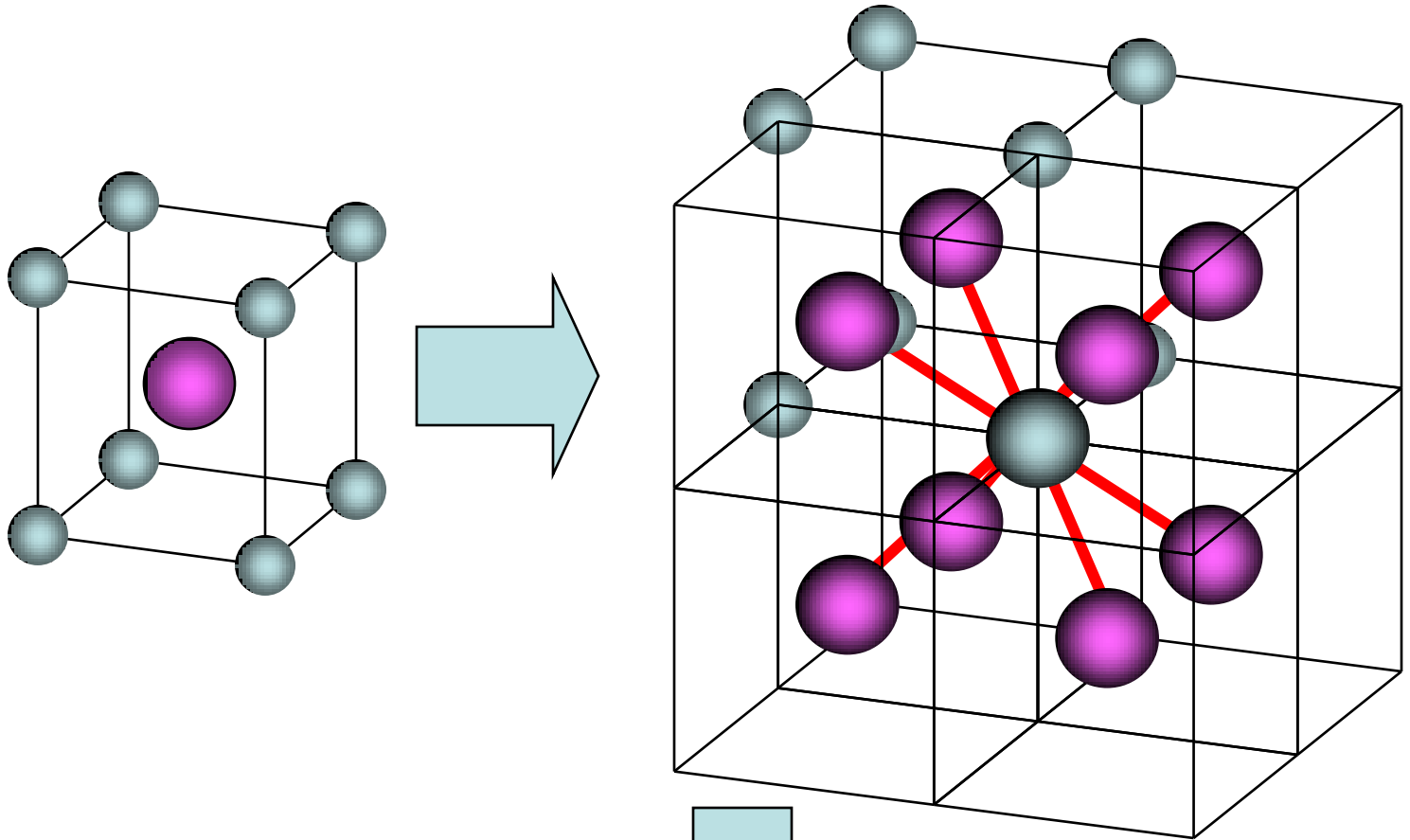
1/8 atom

1 atom

$$\begin{aligned} \text{number of atoms} &= \frac{1}{8} \times 8 \text{ corner atoms} \\ &+ 1 \text{ interior atom} \\ &= 2 \text{ atoms} \end{aligned}$$



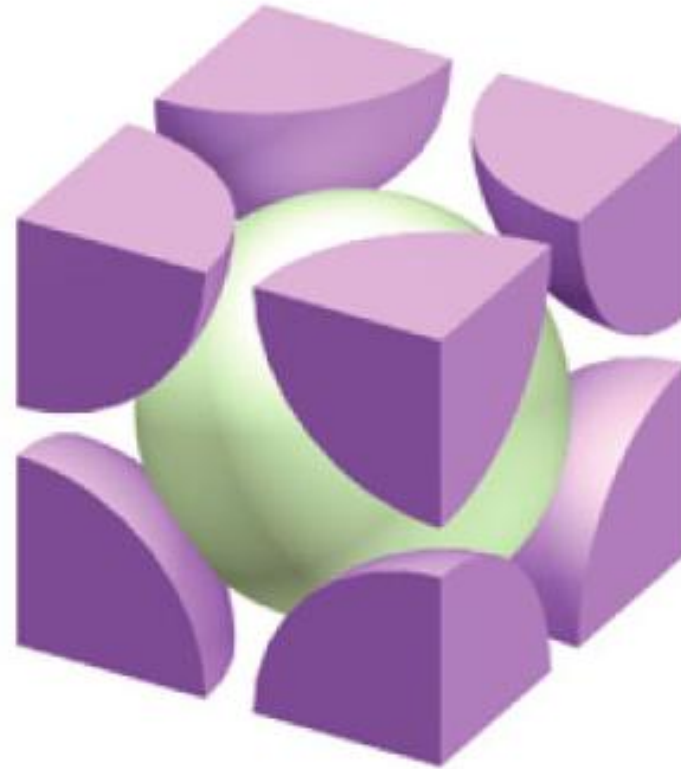
# Coordination Number of BCC



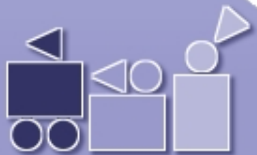
CN OF BCC = 8



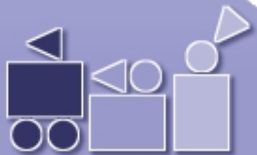
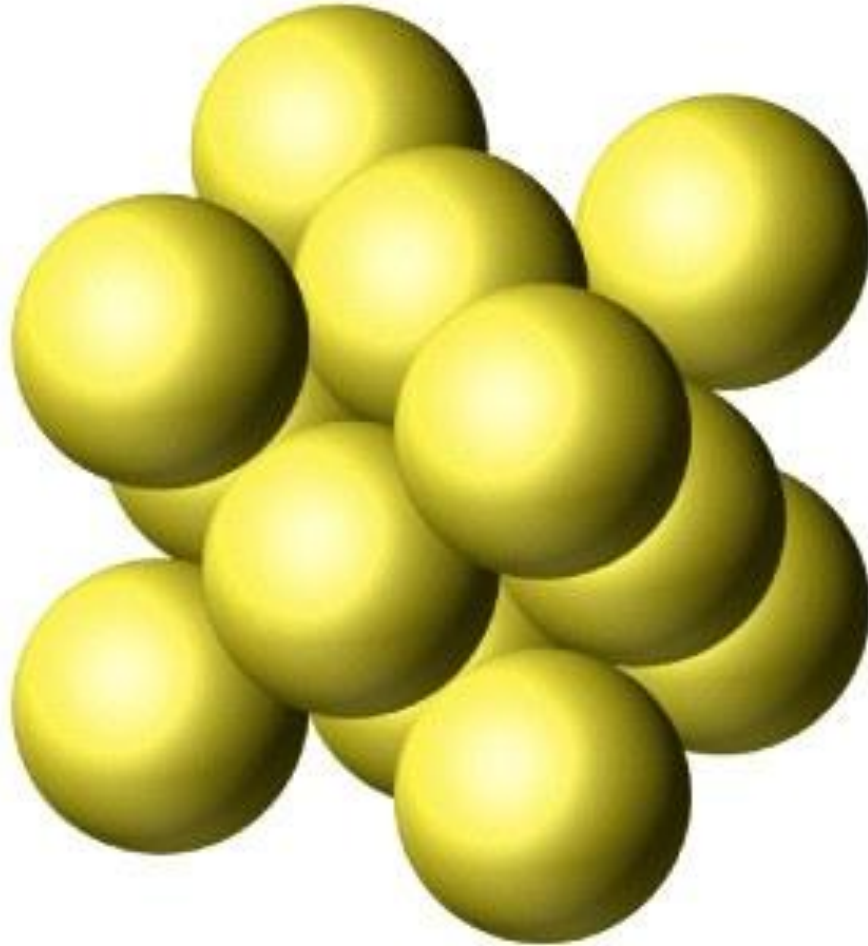
# Packing Efficiency of BCC



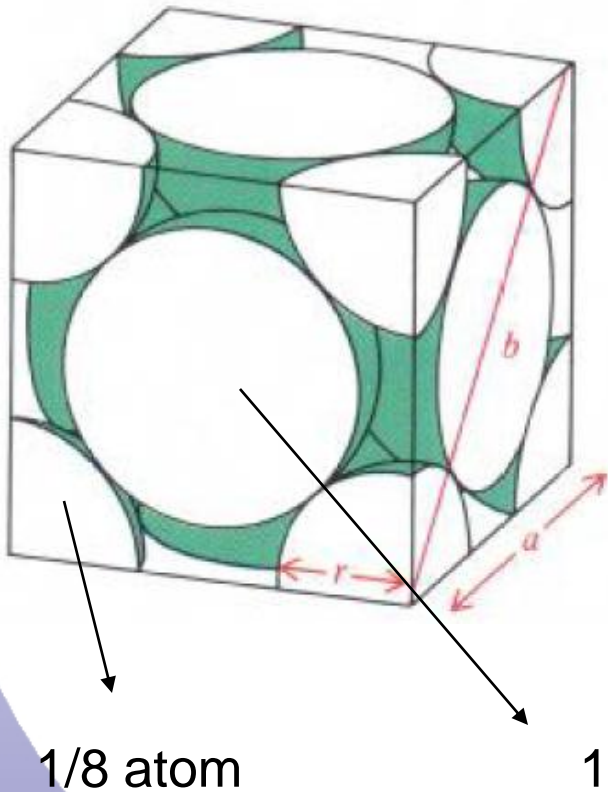
Packing efficiency = 68% ?



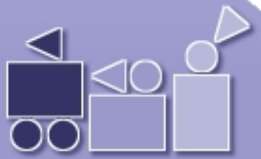
# Number of Atoms in FCC Unit Cell



# Number of Atoms in FCC Unit Cell

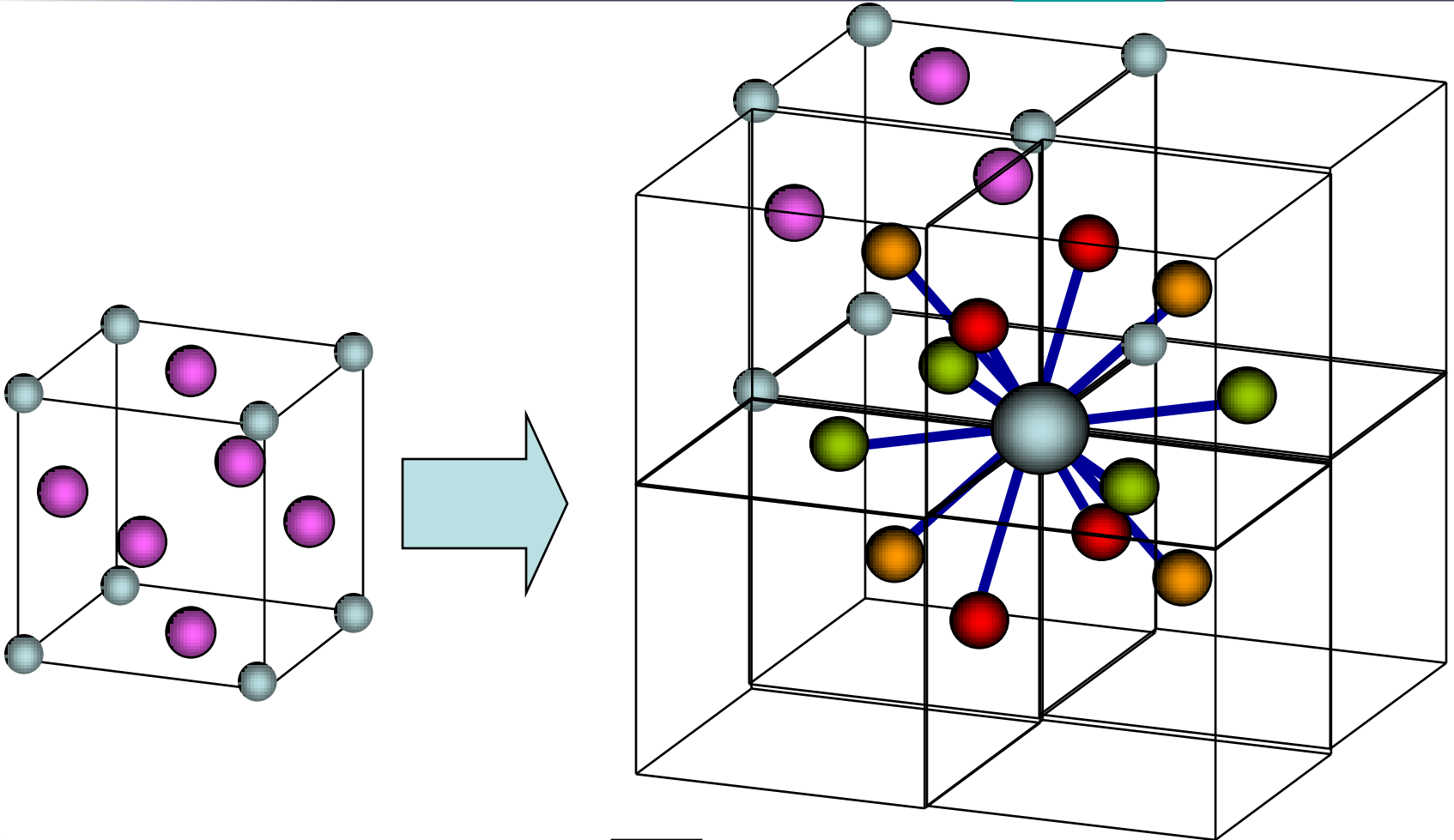


$$\begin{aligned} \text{number of atoms} &= \frac{1}{8} \times 8 \text{ corner atoms} \\ &+ \frac{1}{2} \times 6 \text{ face atoms} \\ &= 4 \text{ atoms} \end{aligned}$$

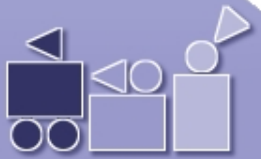




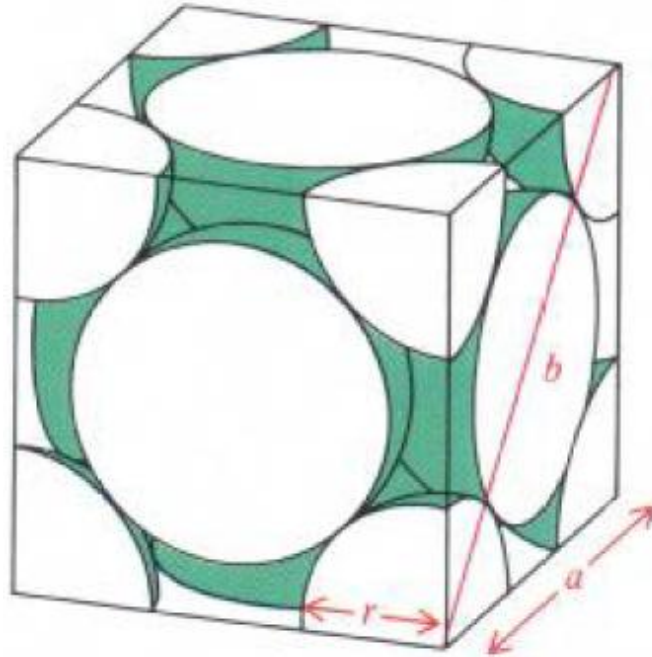
# Coordination Number of FCC



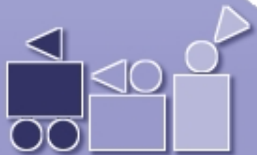
CN OF FCC = 12



# Packing Efficiency of FCC



Packing efficiency = 74% ?



# Keep in mind !!!

Crystal lattice	Number of atoms	Coordination number	Lattice parameter
SC	1	6	$a = 2R$
BCC	2	8	$a\sqrt{3} = 4R$
FCC	4	12	$a\sqrt{2} = 4R$



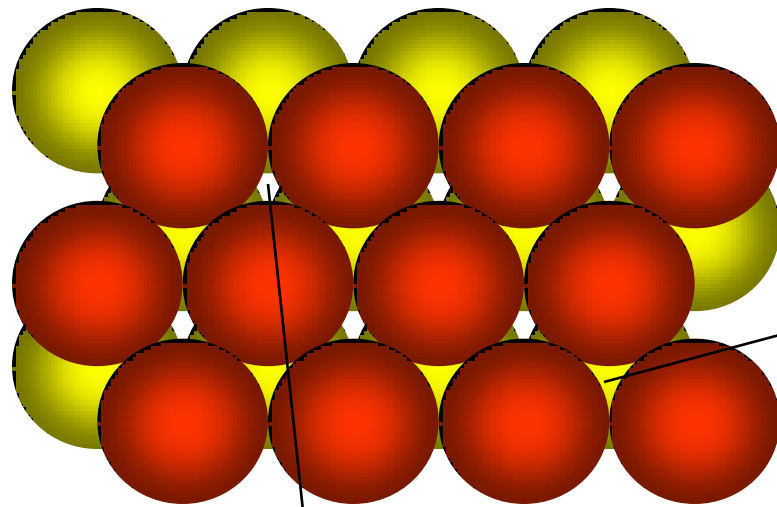
holes in close packed

1. TETRAHEDRAL HOLE

1. OCTAHEDRAL HOLE



# Holes in Close Packed

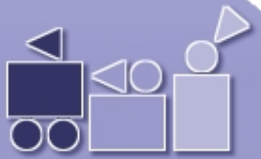
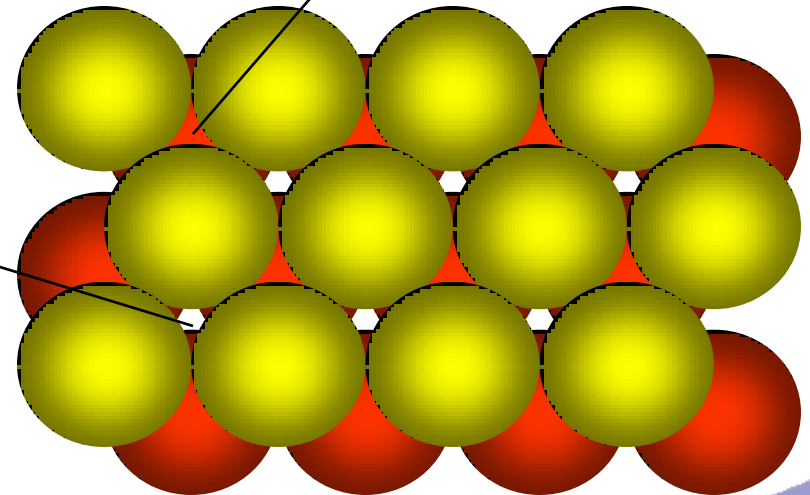


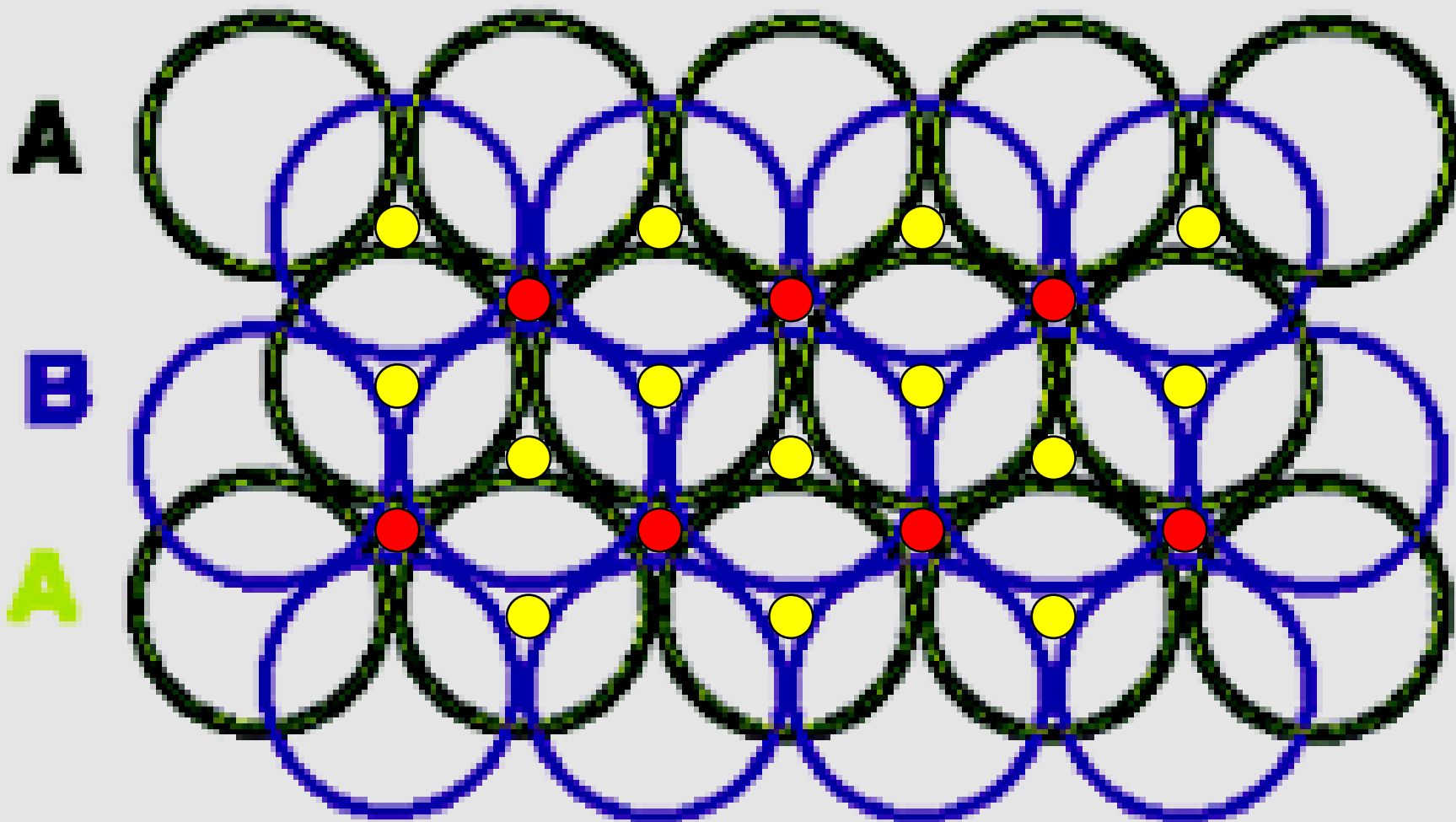
Same hole

Octahedral hole

Tetrahedral hole

Different hole

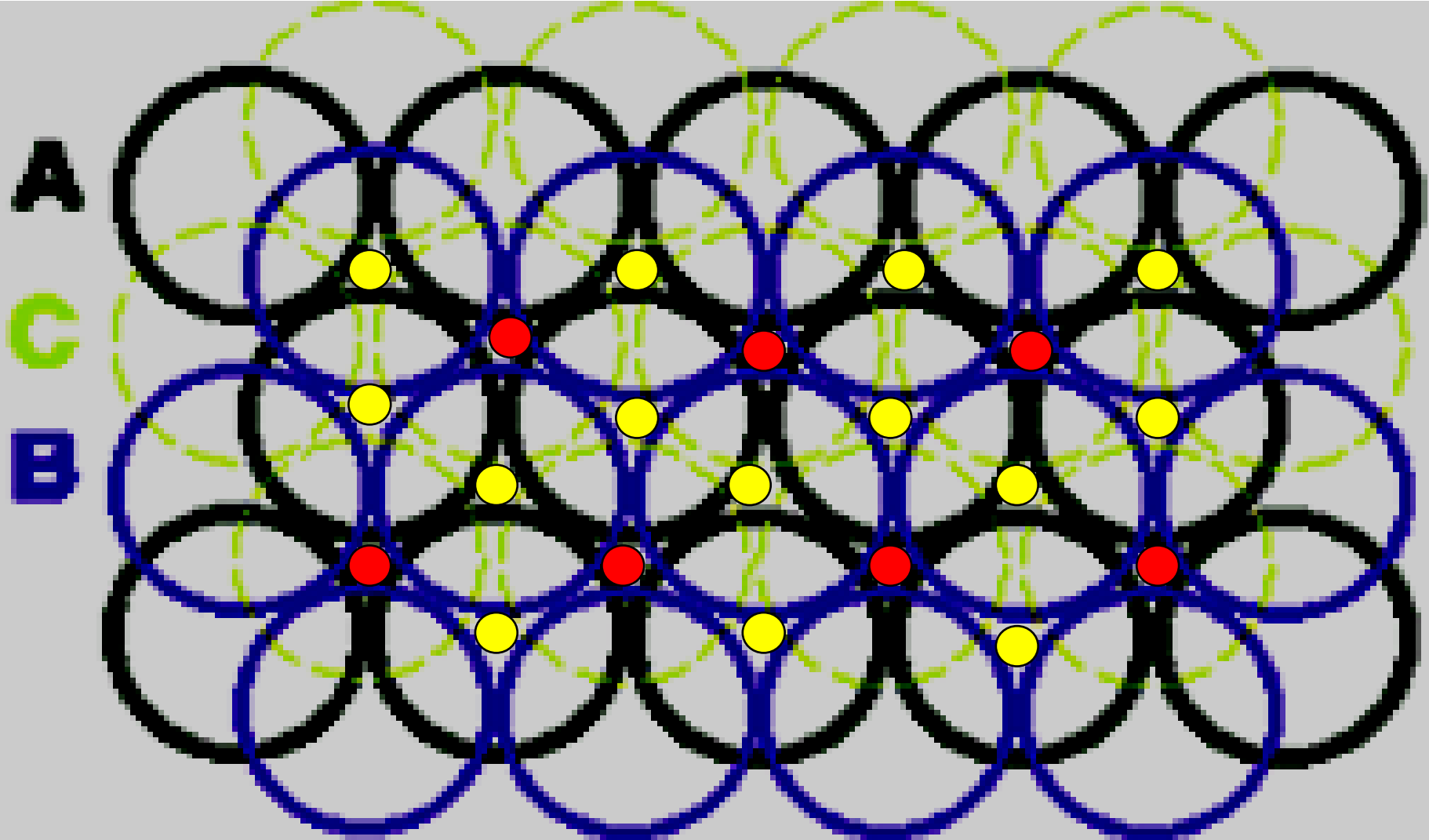




● = Octahedral hole = 7  
 ● = Tetrahedral hole = 14

} tetrahedral hole 2X octahedral hole





● = Octahedral hole = 7  
● = Tetrahedral hole = 14
 } tetrahedral hole 2X octahedral hole



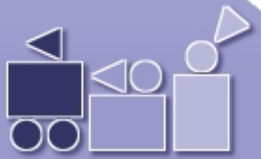
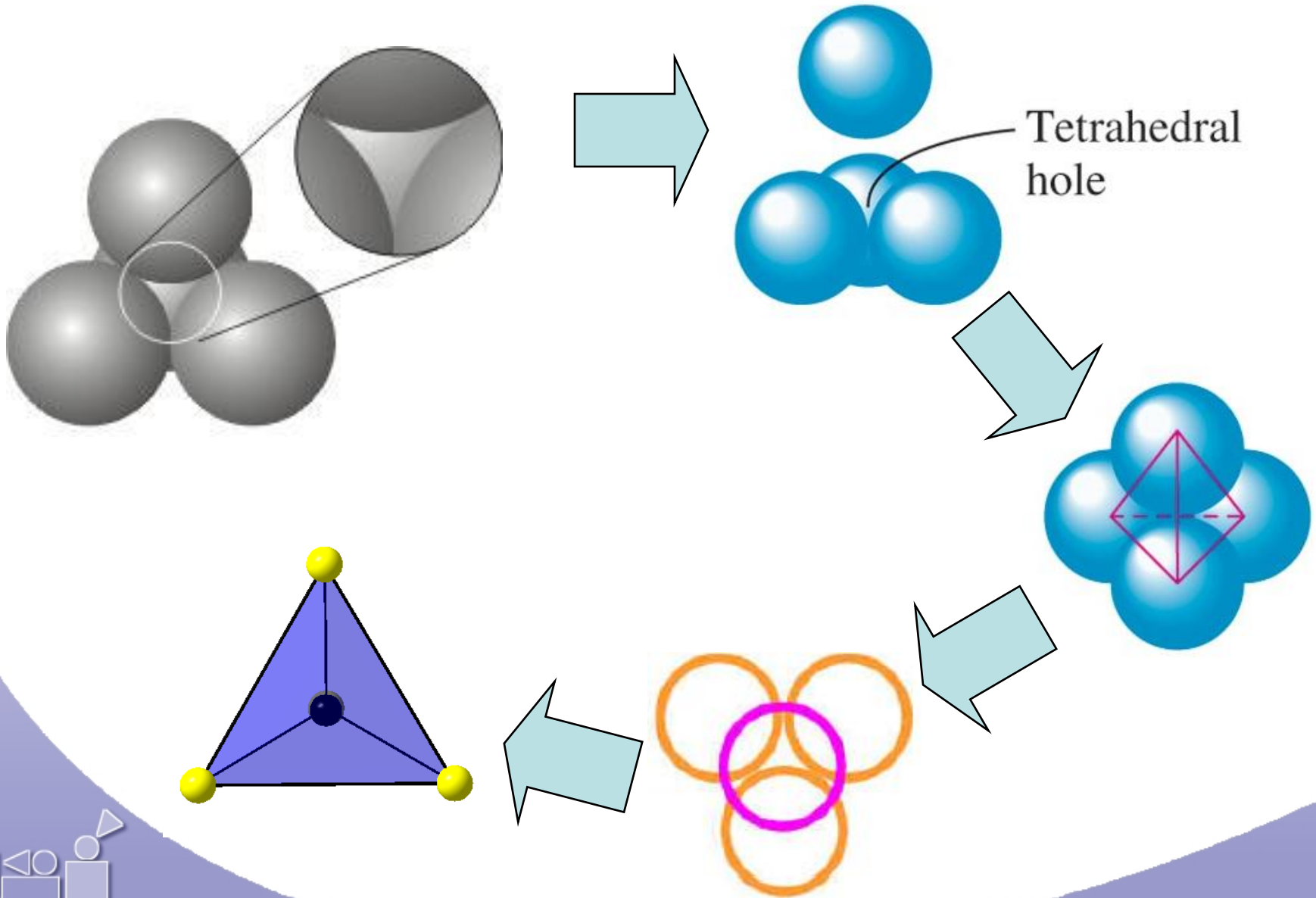
# Tetrahedral hole

- Formed by a planar triangle of atoms, with a 4<sup>th</sup> atom covering the indentation in the center.
- The coordination number of an atom occupying an tetrahedral hole is 4.





# Tetrahedral hole

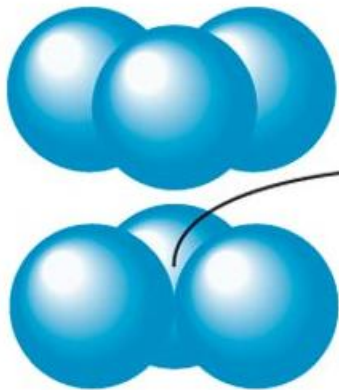
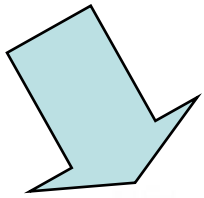
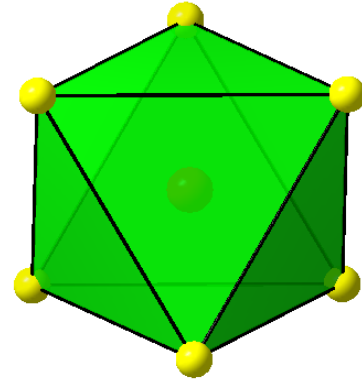
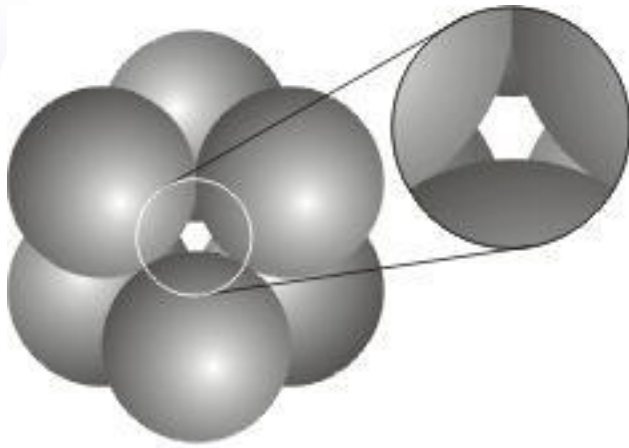


# Octahedral hole

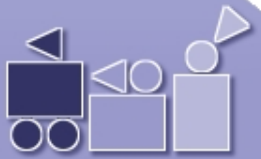
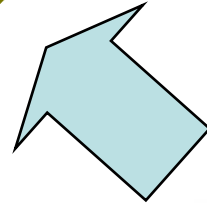
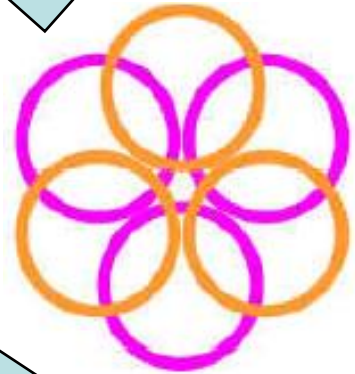
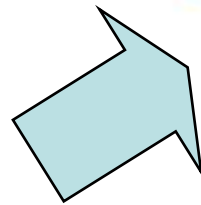
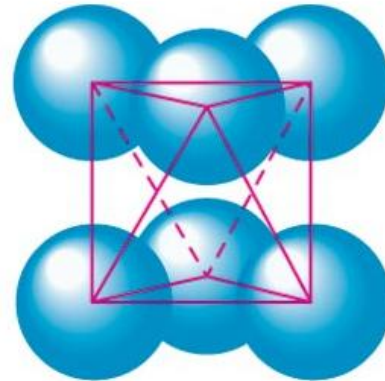
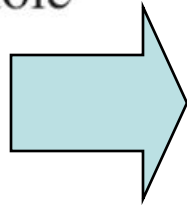
- Lies within two staggered triangular planes of atoms.
- The coordination number of an atom occupying an octahedral hole is 6.



# Octahedral hole



Octahedral hole



# Crystal density

Crystal density determined by:

$$\rho = \frac{\sum n_i \times M}{N_A \times V}$$

Which:

$\rho$  = crystal density (g.cm<sup>-3</sup>)

$n_i$  = number of atoms per unit cell (atoms)

$M$  = molar mass of element (gram.mol<sup>-1</sup>)

$N_A$  = Avogadro number (6.02x10<sup>23</sup>  
atoms.mol<sup>-1</sup>)

$V$  = volume of unit cell (cm<sup>3</sup>)



## Problem 2

- Calculate the density (in  $\text{gram.cm}^{-3}$ ) of platinum metal if it has a face centered cubic unit cell and a crystallographic radius of 135 pm (molar mass of platinum =  $195.1 \text{ gram.mol}^{-1}$ )



- Answer
  - fcc = 4 atoms per unit cell
  - Lattice parameter =  $a$
  - In fcc  $\rightarrow a\sqrt{2} = 4R \rightarrow a = 2R\sqrt{2}$



$$\begin{aligned} - V_{\text{cell}} &= a^3 \\ &= (2R\sqrt{2})^3 \\ &= (2 \times 135 \cdot 10^{-10} \cdot \sqrt{2})^3 \text{ cm}^3 \\ &= 5.567 \times 10^{-23} \text{ cm}^3 \end{aligned}$$

$$\rho = \frac{\sum n_i \times M}{N_A \times V}$$

$$\rho = \frac{4 \text{ atoms} \times 195.1 \text{ gram.mol}^{-1}}{(6.02 \times 10^{23} \text{ atoms.mol}^{-1}) (5.567 \times 10^{-23} \text{ cm}^3)}$$

$$\rho = \frac{780.4 \text{ g}}{33.513 \text{ cm}^3} = 23.28 \text{ g.cm}^{-3}$$



## Problem 3

- Assume the radius of one iron atom is 1.24 angstroms (1 angstrom =  $1 \times 10^{-8}$  cm). What would be the density of body centered cubic (BCC) iron in grams/cubic centimeter? Molar mass of iron =  $55.85 \text{ gram.mol}^{-1}$





- Hint: Find the mass and volume of one unit cell.
- Remember to count only the fraction of each atom in the cell.



- Answer

- bcc = 2 atoms per unit cell

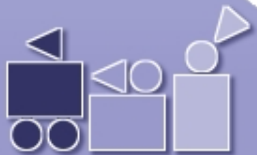
- In bcc:

$$a\sqrt{3} = 4R$$

$$a = \frac{4}{3} R \sqrt{3}$$

$$a = \frac{4}{3} 1.24 \times 10^{-8} \text{ cm} \cdot \sqrt{3}$$

$$= 2.86 \times 10^{-8} \text{ cm}$$



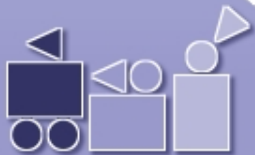
$$\begin{aligned} -V \text{ cell} &= a^3 \\ &= (2.86 \times 10^{-8} \text{ cm})^3 \\ &= 2.34 \times 10^{-23} \text{ cm}^3 \end{aligned}$$



$$\begin{aligned}\text{mass of iron} &= \frac{2 \text{ atoms} \times 55.85 \text{ gram.mol}^{-1}}{6.02 \times 10^{23} \text{ atom.mol}^{-1}} \\ &= 1.85 \times 10^{-22} \text{ gram}\end{aligned}$$

$$\rho = \frac{\text{mass}}{\text{volume}}$$

$$\begin{aligned}&= \frac{1.85 \times 10^{-22} \text{ gram}}{2.34 \times 10^{-23} \text{ atom.mol}^{-1}} \\ &= 7.91 \text{ g.cm}^{-3}\end{aligned}$$



## Problem 4

- Polonium (molar mass = 209 gram.mol<sup>-1</sup>) metal crystallizes in a simple cubic structure.
  - Calculate the density (in gram.cm<sup>-3</sup>) of the polonium metal if the atom radius is 176 pm.
  - Based on a literature density of 9.196 g cm<sup>-3</sup>, what is the radius of Po(in pm)?



## Problem 5

- The radius of the copper atom is 127.8 pm, and its' density is  $8.95 \text{ g/cm}^3$ . Which unit cell is consistent with these data: sc, bcc, or fcc? (molar mass of Cu =  $63.55 \text{ gram.mol}^{-1}$ )



## Problem 6

Below  $1000^{\circ}\text{C}$  Fe crystallizes in a body-centred cubic unit cell with an edge length of  $0.28664\text{ nm}$ .

Above  $1000^{\circ}\text{C}$  Fe forms a face-centred cubic cell with an edge length of  $0.363\text{ nm}$ .

- Determine the density of Fe under these conditions (in  $\text{gram}/\text{cm}^3$ ).
- Which one is denser, bcc or fcc?
- Compared to the packing efficiency, predict how it could be?



# The end of the discussion Of Close Packing Geometry

